**Instructions.** Read the Homework Guide to make sure you understand how to successfully complete the assignment. All claims must be sufficiently justified.

**Definition 1.** See Example 3.15 (in Section 3.2) for the definition of the quaternion group  $Q_8$ . (You will need this group in several exercises below.)

Exercise 1. Complete the following exercises from Section 9.4:

# \*11, 17, 19 (just the first part, and see Example 9.25), 22, 24, 25, 48, \*\*55

**Exercise 2.** Suppose G is the internal direct products of the subgroups H and K. Prove that G isomorphic to  $H \times K$ .

**Exercise 3.** Complete the following exercises from Section 10.4:

# 1, **\*2**, 3, 4, 5, 10, **\*11**